# AMENDMENTS TO THE CLAIMS

This listing of claims will replace all prior versions and listings of claims in the application:

# LISTING OF CLAIMS:

1. (original) A method for an optimal one-shot phase and frequency estimation for timing acquisition for signals transmitted over a communications channel, the method comprising:

sampling a preamble comprising a known string of data bits;

estimating the sampled preamble ( $\bar{Y}$ ), the estimated preamble further comprising an estimated amplitude ( $\hat{A}$ ), an estimated frequency ( $\hat{f}$ ), and an estimated phase ( $\hat{\Phi}$ );

calculating a cost function  $(C(\hat{f}, \hat{\Phi}))$  as a function of the estimated frequency  $(\hat{f})$  and the estimated phase  $(\hat{\Phi})$ ;

varying at least one of the estimated frequency  $(\hat{f})$  or estimated phase  $(\hat{\Phi})$  to calculate a plurality of cost functions; and

selecting the cost function  $(C(\hat{f}, \hat{\Phi}))$  having a minimum value, wherein said cost function having the minimum value is a function of an optimal estimated frequency  $(\hat{f})$  and an optimal estimated phase  $(\hat{\Phi})$ .

2. (original) The method of claim 1, wherein the preamble is sinusoidal.

- 3. (original) The method of claim 1, wherein the preamble is sampled once for each data bit in the preamble.
- 4. (original) The method of claim 1, wherein the sampling comprises the following calculation:

 $\vec{X} = [x_0 \cdots x_N]$  where  $x_k = A \sin(\Phi + k \cdot f \cdot \frac{\pi}{2}) + n_k$ , A is an amplitude value,  $\Phi$  is a phase value, f is a frequency value, and  $n_k$  is a noise component of a  $k^{th}$  sample.

5. (original) The method of claim 1, wherein the estimating the sampled preamble comprises the following calculation:

$$\vec{Y} = [y_0 \cdots y_N]$$
 where  $y_k = \hat{A} \sin \left( \hat{\Phi} + k \cdot \hat{f} \cdot \frac{\pi}{2} \right)$ .

- 6. (original) The method of claim 5, wherein the noise component of the sampled preamble has a standard deviation  $(\sigma)$ .
- 7. (original) The method of claim 6, wherein the frequency value of the sampled preamble has a normal distribution having a standard deviation  $(\sigma_f)$ .
- 8. (original) The method of claim 7, wherein the calculating comprises the following:

$$C(\hat{f}, \hat{\Phi}) = \hat{A}^2 \sum_{k=0}^{N-1} \sin^2 \left( \hat{\Phi} + k \cdot \hat{f} \cdot \frac{\pi}{2} \right) - 2\hat{A} \sum_{k=0}^{N-1} x_k \sin \left( \hat{\Phi} + k \cdot \hat{f} \cdot \frac{\pi}{2} \right) + \frac{\sigma^2 \cdot \left( \hat{f} - \bar{f} \right)^2}{\sigma_f^2}, \text{ where } \bar{f}$$

- 9. (original) The method of claim 8, wherein each of the plurality of cost functions is calculated with a different frequency value  $(\hat{f})$  and a different phase value  $(\hat{\Phi})$ .
- 10. (original) The method of claim 9, wherein the plurality of cost functions are calculated substantially simultaneously.
- 11. (original) The method of claim 1, wherein selecting the minimum value cost function further comprises selecting a plurality of first minimum cost functions such that each of the first minimum cost functions has a different estimated frequency  $(\hat{f})$ .
- (original) The method of claim 11, wherein selecting the minimum value cost function further comprises selecting a second minimum cost function from the plurality of first minimum cost functions, and wherein the second minimum cost function is a function of an optimal estimated frequency  $(\hat{f})$  and an optimal estimated phase  $(\hat{\Phi})$ .
- (original) The method of claim 1, wherein selecting the minimum value cost function further comprises selecting a plurality of first minimum cost functions such that each of the first minimum cost functions has a different estimated phase  $(\hat{\Phi})$ .
- 14. (original) The method of claim 13, wherein selecting the minimum value cost function further comprises selecting a second minimum cost function from the plurality of first minimum cost functions, and wherein the second minimum cost function is a function of an optimal estimated frequency  $(\hat{f})$  and an optimal estimated phase  $(\hat{\Phi})$ .

15. (original) A communications channel for an optimal one-shot phase and frequency estimation for timing acquisition for signals transmitted over the communications channel, the communications channel comprising:

a sampler for sampling a preamble comprising a known string of data bits;

a first calculator for estimating the sampled preamble  $(\vec{Y})$ , the estimated preamble further comprising an estimated amplitude  $(\hat{A})$ , an estimated frequency  $(\hat{f})$ , and an estimated phase  $(\hat{\Phi})$ ;

a second calculator for calculating a plurality of cost functions  $(C(\hat{f}, \hat{\Phi}))$  as a function of the estimated frequency  $(\hat{f})$  and the estimated phase  $(\hat{\Phi})$  by varying at least one of the estimated frequency  $(\hat{f})$  or estimated phase  $(\hat{\Phi})$ ; and

a selector for determining the cost function  $(C(\hat{f}, \hat{\Phi}))$  having a minimum value, wherein said cost function having the minimum value is a function of an optimal estimated frequency  $(\hat{f})$  and an optimal estimated phase  $(\hat{\Phi})$ .

- 16. (original) The communications channel of claim 15, wherein the preamble is sinusoidal.
- 17. (original) The communications channel of claim 15, wherein the sampler samples the preamble once for each data bit in the preamble.
- 18. (original) The communications channel of claim 15, wherein the sampler samples the preamble in accordance with the following calculation:

 $\vec{X} = \left[x_0 \cdots x_N\right]$  where  $x_k = A \sin\left(\Phi + k \cdot f \cdot \frac{\pi}{2}\right) + n_k$ , A is an amplitude value,  $\Phi$  is a phase value, f is a frequency value, and  $n_k$  is a noise component of a  $k^{th}$  sample.

19. (original) The communications channel of claim 15, wherein the first calculator estimates the sampled preamble in accordance with the following calculation:

$$\vec{Y} = [y_0 \cdots y_N] \text{ where } y_k = \hat{A} \sin \left(\hat{\Phi} + k \cdot \hat{f} \cdot \frac{\pi}{2}\right).$$

- 20. (original) The communications channel of claim 19, wherein the noise component of the sampled preamble has a standard deviation ( $\sigma$ ).
- 21. (original) The communications channel of claim 20, wherein the frequency value of the sampled preamble has a normal distribution having a standard deviation  $(\sigma_f)$ .
- 22. (original) The communications channel of claim 21, wherein the second calculator calculates the plurality of cost functions in accordance with the following:

$$C(\hat{f}, \hat{\Phi}) = \hat{A}^2 \sum_{k=0}^{N-1} \sin^2 \left( \hat{\Phi} + k \cdot \hat{f} \cdot \frac{\pi}{2} \right) - 2\hat{A} \sum_{k=0}^{N-1} x_k \sin \left( \hat{\Phi} + k \cdot \hat{f} \cdot \frac{\pi}{2} \right) + \frac{\sigma^2 \cdot \left( \hat{f} - \bar{f} \right)^2}{\sigma_f^2}, \text{ where } \bar{f}$$

is a nominal frequency.

(original) The communications channel of claim 22, wherein each of the plurality of cost functions is calculated with a different frequency value  $(\hat{f})$  and a different phase value  $(\hat{\Phi})$ .

- 24. (original) The communications channel of claim 23, wherein the plurality of cost functions are calculated substantially simultaneously.
- 25. (original) The communications channel of claim 15, wherein the selector determines the minimum value cost function by selecting a plurality of first minimum cost functions such that each of the first minimum cost functions has a different estimated frequency  $(\hat{f})$
- 26. (original) The communications channel of claim 25, wherein the selector determines the minimum value cost function by selecting a second minimum cost function from the plurality of first minimum cost functions, and wherein the second minimum cost function is a function of an optimal estimated frequency  $(\hat{f})$  and an optimal estimated phase  $(\hat{\Phi})$ .
- 27. (original) The communications channel of claim 15, wherein the selector determines the minimum value cost function by selecting a plurality of first minimum cost functions such that each of the first minimum cost functions has a different estimated phase (Φ̂).
- 28. (original) The communications channel of claim 27, wherein the selector determines the minimum value cost function by selecting a second minimum cost function from the plurality of first minimum cost functions, and wherein the second minimum cost function is a function of an optimal estimated frequency  $(\hat{f})$  and an optimal estimated phase  $(\hat{\Phi})$ .
- 29. (original) A disk drive system for an optimal one-shot phase and frequency estimation for timing acquisition for signals transmitted over a communications channel, the system comprising:

rotating magnetic media for storing data;
a motor for rotating the magnetic media;
a recording head for transmitting data;
an actuator for positioning the recording head; and

a communications channel for communicating data to be stored on or read from the recording media, wherein the communications channel further comprises a sampler for sampling a preamble comprising a known string of data bits, a first calculator for estimating the sampled preamble  $(\vec{Y})$ , a second calculator for calculating a plurality of cost functions  $(C(\hat{f}, \hat{\Phi}))$  as a function of the estimated frequency  $(\hat{f})$  and the estimated phase  $(\hat{\Phi})$  by varying at least one of the estimated frequency  $(\hat{f})$  or estimated phase  $(\hat{\Phi})$ , and a selector for determining the cost function  $(C(\hat{f}, \hat{\Phi}))$  having a minimum value, wherein said cost function having the minimum value is a function of an optimal estimated frequency  $(\hat{f})$  and an optimal estimated phase  $(\hat{\Phi})$ , and wherein the estimated preamble further comprises an estimated amplitude  $(\hat{A})$ , an estimated frequency  $(\hat{f})$ , and an estimated phase  $(\hat{\Phi})$ 

- 30. (original) The system of claim 29, wherein the preamble is sinusoidal.
- 31. (original) The system of claim 29, wherein the sampler samples the preamble once for each data bit in the preamble.

- 32. (original) The system of claim 29, wherein the sampler samples the preamble in accordance with the following calculation:  $\vec{X} = \left[x_0 \cdots x_N\right] \text{ where } x_k = A \sin\left(\Phi + k \cdot f \cdot \frac{\pi}{2}\right) + n_k, A \text{ is an amplitude value, } \Phi \text{ is a phase value, } f \text{ is a frequency value, and } n_k \text{ is a noise component of a } k^{th} \text{ sample.}$
- 33. (original) The system of claim 29, wherein the first calculator estimates the sampled preamble in accordance with the following calculation:

$$\vec{Y} = [y_0 \cdots y_N] \text{ where } y_k = \hat{A} \sin \left(\hat{\Phi} + k \cdot \hat{f} \cdot \frac{\pi}{2}\right).$$

- 34. (original) The system of claim 33, wherein the noise component of the sampled preamble has a standard deviation  $(\sigma)$ .
- 35. (original) The system of claim 34, wherein the frequency value of the sampled preamble has a normal distribution having a standard deviation  $(\sigma_f)$ .
- 36. (original) The system of claim 35, wherein the second calculator calculates the cost functions in accordance with the following:

$$C(\hat{f}, \hat{\Phi}) = \hat{A}^2 \sum_{k=0}^{N-1} \sin^2 \left( \hat{\Phi} + k \cdot \hat{f} \cdot \frac{\pi}{2} \right) - 2\hat{A} \sum_{k=0}^{N-1} x_k \sin \left( \hat{\Phi} + k \cdot \hat{f} \cdot \frac{\pi}{2} \right) + \frac{\sigma^2 \cdot \left( \hat{f} - \bar{f} \right)^2}{\sigma_f^2}, \text{ where } \bar{f}$$

is a nominal frequency.

37. (original) The system of claim 36, wherein each of the plurality of cost functions is calculated with a different frequency value  $(\hat{f})$  and a different phase value  $(\hat{\Phi})$ .

- 38. (original) The system of claim 37, wherein the plurality of cost functions are calculated substantially simultaneously.
- 39. (original) The system of claim 29, wherein the selector determines the minimum value cost function by selecting a plurality of first minimum cost functions such that each of the first minimum cost functions has a different estimated frequency ( $\hat{f}$ ).
- 40. (original) The system of claim 39, wherein the selector determines the minimum value cost function by selecting a second minimum cost function from the plurality of first minimum cost functions, and wherein the second minimum cost function is a function of an optimal estimated frequency  $(\hat{f})$  and an optimal estimated phase  $(\hat{\Phi})$ .
- (original) The system of claim 29, wherein the selector determines the cost minimum value function by selecting a plurality of first minimum cost functions such that each of the first minimum cost functions has a different estimated phase ( $\hat{\Phi}$ ).
- 42. (original) The system of claim 41, wherein the selector determines the minimum value cost function by selecting a second minimum cost function from the plurality of first minimum cost functions, and wherein the second minimum cost function is a function of an optimal estimated frequency  $(\hat{f})$  and an optimal estimated phase  $(\hat{\Phi})$ .
- 43. (original) A communications channel for an optimal one-shot phase and frequency estimation for timing acquisition for signals transmitted over the communications channel, the communications channel comprising:

a means for sampling a preamble comprising a known string of data bits;

a means for estimating the sampled preamble  $(\bar{Y})$ , the estimated preamble further comprising an estimated amplitude  $(\hat{A})$ , an estimated frequency  $(\hat{f})$ , and an estimated phase  $(\hat{\Phi})$ ;

a means for calculating a plurality of cost functions  $(C(\hat{f}, \hat{\Phi}))$  as a function of the estimated frequency  $(\hat{f})$  and the estimated phase  $(\hat{\Phi})$  by varying at least one of the estimated frequency  $(\hat{f})$  or estimated phase  $(\hat{\Phi})$ ; and

a means for selecting the cost function  $(C(\hat{f}, \hat{\Phi}))$  having a minimum value, wherein said cost function having the minimum value is a function of an optimal estimated frequency  $(\hat{f})$  and an optimal estimated phase  $(\hat{\Phi})$ .

- 44. (original) The communications channel of claim 43, wherein the preamble is sinusoidal.
- 45. (original) The communications channel of claim 43, wherein the preamble is sampled once for each data bit in the preamble.
- 46. (original) The communications channel of claim 43, wherein the means for sampling samples the preamble in accordance with the following calculation:  $\vec{X} = \left[x_0 \cdots x_N\right] \text{ where } x_k = A \sin\left(\Phi + k \cdot f \cdot \frac{\pi}{2}\right) + n_k, A \text{ is an amplitude value, } \Phi \text{ is a phase value, } f \text{ is a frequency value, and } n_k \text{ is a noise component of a } k^{th} \text{ sample.}$

47. (original) The communications channel of claim 43, wherein the means for estimating estimates the sampled preamble in accordance with the following calculation:

$$\vec{Y} = [y_0 \cdots y_N]$$
 where  $y_k = \hat{A} \sin \left( \hat{\Phi} + k \cdot \hat{f} \cdot \frac{\pi}{2} \right)$ .

- 48. (original) The communications channel of claim 47, wherein the noise component of the sampled preamble has a standard deviation  $(\sigma)$ .
- 49. (original) The communications channel of claim 48, wherein the frequency value of the sampled preamble has a normal distribution having a standard deviation  $(\sigma_f)$ .
- 50. (original) The communications channel of claim 49, wherein the means for calculating calculates the cost function in accordance with the following:

$$C(\hat{f}, \hat{\Phi}) = \hat{A}^2 \sum_{k=0}^{N-1} \sin^2 \left( \hat{\Phi} + k \cdot \hat{f} \cdot \frac{\pi}{2} \right) - 2\hat{A} \sum_{k=0}^{N-1} x_k \sin \left( \hat{\Phi} + k \cdot \hat{f} \cdot \frac{\pi}{2} \right) + \frac{\sigma^2 \cdot \left( \hat{f} - \bar{f} \right)^2}{\sigma_f^2}, \text{ where } \bar{f}$$

- (original) The communications channel of claim 50, wherein each of the plurality of cost functions is calculated with a different frequency value  $(\hat{f})$  and a different phase value  $(\hat{\Phi})$ .
- 52. (original) The communications channel of claim 51, wherein the plurality of cost functions are calculated substantially simultaneously.
- 53. (original) The communications channel of claim 43, wherein means for selecting selects the minimum value cost function by selecting a plurality of first minimum cost functions

such that each of the first minimum cost functions has a different estimated frequency  $(\hat{f})$ .

- 54. (original) The communications channel of claim 53, wherein the means for selecting selects the minimum value cost function by selecting a second minimum cost function from the plurality of first minimum cost functions, and wherein the second minimum cost function is a function of an optimal estimated frequency  $(\hat{f})$  and an optimal estimated phase  $(\hat{\Phi})$ .
- 55. (original) The communications channel of claim 43, wherein the means for selecting selects the minimum value cost function by selecting a plurality of first minimum cost functions such that each of the first minimum cost functions has a different estimated phase  $(\hat{\Phi})$ .
- 56. (original) The communications channel of claim 55, wherein the means for selecting selects the minimum value cost function by selecting a second minimum cost function from the plurality of first minimum cost functions, and wherein the second minimum cost function is a function of an optimal estimated frequency  $(\hat{f})$  and an optimal estimated phase  $(\hat{\Phi})$ .
- 57. (original) A computer program product containing a program for providing an optimal one-shot phase and frequency estimation for timing acquisition for signals transmitted over a communications channel, the program comprising:

sampling a preamble comprising a known string of data bits;

estimating the sampled preamble  $(\bar{Y})$ , the estimated preamble further comprising an estimated amplitude  $(\hat{A})$ , an estimated frequency  $(\hat{f})$ , and an estimated phase  $(\hat{\Phi})$ ;

calculating a cost function  $(C(\hat{f}, \hat{\Phi}))$  as a function of the estimated frequency  $(\hat{f})$  and the estimated phase  $(\hat{\Phi})$ ;

varying at least one of the estimated frequency  $(\hat{f})$  or estimated phase  $(\hat{\Phi})$  to calculate a plurality of cost functions; and

selecting the cost function  $(C(\hat{f}, \hat{\Phi}))$  having a minimum value, wherein said cost function having the minimum value is a function of an optimal estimated frequency  $(\hat{f})$  and an optimal estimated phase  $(\hat{\Phi})$ .

- 58. (original) The computer program product of claim 57, wherein the preamble is sinusoidal.
- 59. (original) The computer program product of claim 57, wherein the preamble is sampled once for each data bit in the preamble.
- 60. (original) The computer program product of claim 57, wherein the sampling comprises
  the following calculation:

 $\vec{X} = [x_0 \cdots x_N]$  where  $x_k = A \sin \left( \Phi + k \cdot f \cdot \frac{\pi}{2} \right) + n_k$ , A is an amplitude value,  $\Phi$  is a phase value, f is a frequency value, and  $n_k$  is a noise component of a  $k^{th}$  sample.

61. (original) The computer program product of claim 57, wherein the estimating the sampled preamble comprises the following calculation:

$$\vec{Y} = [y_0 \cdots y_N] \text{ where } y_k = \hat{A} \sin \left( \hat{\Phi} + k \cdot \hat{f} \cdot \frac{\pi}{2} \right).$$

- 62. (currently amended) The computer program product of claim 51 57, wherein the noise component of the sampled preamble has a standard deviation  $(\sigma)$ .
- 63. (original) The computer program product of claim 62, wherein the frequency value of the sampled preamble has a normal distribution having a standard deviation  $(\sigma_f)$ .
- 64. (original) The computer program product of claim 63, wherein the calculating comprises the following:

$$C(\hat{f}, \hat{\Phi}) = \hat{A}^{2} \sum_{k=0}^{N-1} \sin^{2} \left( \hat{\Phi} + k \cdot \hat{f} \cdot \frac{\pi}{2} \right) - 2\hat{A} \sum_{k=0}^{N-1} x_{k} \sin \left( \hat{\Phi} + k \cdot \hat{f} \cdot \frac{\pi}{2} \right) + \frac{\sigma^{2} \cdot \left( \hat{f} - \bar{f} \right)^{2}}{\sigma_{f}^{2}}, \text{ where } \bar{f}$$

- (original) The computer program product of claim 64, wherein each of the plurality of cost functions is calculated with a different frequency value  $(\hat{f})$  and a different phase value  $(\hat{\Phi})$ .
- 66. (original) The computer program product of claim 65, wherein the plurality of cost functions are calculated substantially simultaneously.

- 67. (original) The computer program product of claim 57, wherein selecting the minimum value cost function further comprises selecting a plurality of first minimum cost functions such that each of the first minimum cost functions has a different estimated frequency  $(\hat{f})$ .
- 68. (original) The computer program product of claim 67, wherein selecting the minimum value cost function further comprises selecting a second minimum cost function from the plurality of first minimum cost functions, and wherein the second minimum cost function is a function of an optimal estimated frequency  $(\hat{f})$  and an optimal estimated phase  $(\hat{\Phi})$ .
- 69. (original) The computer program product of claim 57, wherein selecting the minimum value cost function further comprises selecting a plurality of first minimum cost functions such that each of the first minimum cost functions has a different estimated phase  $(\hat{\Phi})$ .
- 70. (original) The computer program product of claim 69, wherein selecting the minimum value cost function further comprises selecting a second minimum cost function from the plurality of first minimum cost functions, and wherein the second minimum cost function is a function of an optimal estimated frequency ( $\hat{f}$ ) and an optimal estimated phase ( $\hat{\Phi}$ ).
- (original) A disk drive system for an optimal one-shot phase and frequency estimation for timing acquisition for signals transmitted over a communications channel, the system comprising:

means for storing data;

means for rotating the means for storing;

means for transmitting data to and from the means for storing;

means for positioning the means for transmitting data; and

means for communicating data to be stored on or read from the means for storing, wherein said means for communicating further comprises means for sampling a preamble comprising a known string of data bits, means for estimating the sampled preamble  $(\bar{Y})$ , means for calculating a plurality of cost functions  $(C(\hat{f}, \hat{\Phi}))$  as a function of the estimated frequency  $(\hat{f})$  and the estimated phase  $(\hat{\Phi})$  by varying at least one of the estimated frequency  $(\hat{f})$  or estimated phase  $(\hat{\Phi})$ , and means for determining the cost function  $(C(\hat{f}, \hat{\Phi}))$  having a minimum value, wherein said cost function having the minimum value is a function of an optimal estimated frequency  $(\hat{f})$  and an optimal estimated phase  $(\hat{\Phi})$ , and wherein the estimated preamble further comprises an estimated amplitude  $(\hat{A})$ , an estimated frequency  $(\hat{f})$ , and an estimated phase  $(\hat{\Phi})$ 

- 72. (original) The system of claim 71, wherein the preamble is sinusoidal.
- 73. (original) The system of claim 71, wherein the means for sampling samples the preamble once for each data bit in the preamble.
- 74. (original) The system of claim 71, wherein the means for sampling samples the preamble in accordance with the following calculation:

 $\bar{X} = \left[x_0 \cdots x_N\right]$  where  $x_k = A \sin\left(\Phi + k \cdot f \cdot \frac{\pi}{2}\right) + n_k$ , A is an amplitude value,  $\Phi$  is a phase value, f is a frequency value, and  $n_k$  is a noise component of a  $k^{th}$  sample.

75. (original) The system of claim 71, wherein the means for estimating the sampled preamble in accordance with the following calculation:

$$\vec{Y} = [y_0 \cdots y_N] \text{ where } y_k = \hat{A} \sin \left(\hat{\Phi} + k \cdot \hat{f} \cdot \frac{\pi}{2}\right).$$

- 76. (original) The system of claim 75, wherein the noise component of the sampled preamble has a standard deviation  $(\sigma)$ .
- 77. (original) The system of claim 76, wherein the frequency value of the sampled preamble has a normal distribution having a standard deviation  $(\sigma_f)$ .
- 78. (original) The system of claim 77, wherein the means for calculating calculates the cost functions in accordance with the following:

$$C(\hat{f}, \hat{\Phi}) = \hat{A}^2 \sum_{k=0}^{N-1} \sin^2 \left( \hat{\Phi} + k \cdot \hat{f} \cdot \frac{\pi}{2} \right) - 2\hat{A} \sum_{k=0}^{N-1} x_k \sin \left( \hat{\Phi} + k \cdot \hat{f} \cdot \frac{\pi}{2} \right) + \frac{\sigma^2 \cdot \left( \hat{f} - \bar{f} \right)^2}{\sigma_f^2}, \text{ where } \bar{f}$$

- 79. (original) The system of claim 78, wherein each of the plurality of cost functions is calculated with a different frequency value ( $\hat{f}$ ) and a different phase value ( $\hat{\Phi}$ ).
- 80. (original) The system of claim 79, wherein the plurality of cost functions are calculated substantially simultaneously.

- 81. (original) The system of claim 71, wherein the means for selecting determines the minimum value cost function by selecting a plurality of first minimum cost functions such that each of the first minimum cost functions has a different estimated frequency  $(\hat{f})$ .
- 82. (original) The system of claim 81, wherein the means for selecting determines the minimum value cost function by selecting a second minimum cost function from the plurality of first minimum cost functions, and wherein the second minimum cost function is a function of an optimal estimated frequency  $(\hat{f})$  and an optimal estimated phase  $(\hat{\Phi})$ .
- 83. (original) The system of claim 71, wherein the means for selecting determines the cost minimum value function by selecting a plurality of first minimum cost functions such that each of the first minimum cost functions has a different estimated phase  $(\hat{\Phi})$ .
- 84. (original) The system of claim 83, wherein the means for selecting determines the minimum value cost function by selecting a second minimum cost function from the plurality of first minimum cost functions, and wherein the second minimum cost function is a function of an optimal estimated frequency  $(\hat{f})$  and an optimal estimated phase  $(\hat{\Phi})$ .